

## Lesson 1.12 - 1.16 - Practice Quiz

1) Use long division to divide the following:

a.  $(90r^3 + 145r^2 + 77r + 29) \div (9r + 10)$

$$\begin{array}{r}
 10r^2 + 5r + 3 \\
 9r + 10 \overline{) 90r^3 + 145r^2 + 77r + 29} \\
 \underline{90r^3 + 100r^2} \phantom{+ 77r + 29} \\
 45r^2 + 77r \phantom{+ 29} \\
 \underline{45r^2 + 50r} \phantom{+ 29} \\
 27r + 29 \\
 \underline{27r + 30} \\
 -1
 \end{array}$$

$$10r^2 + 5r + 3 - \frac{1}{9r + 10}$$

b.  $(3b^3 - 14b^2 - 22b + 70) \div (3b + 7)$

$$\begin{array}{r}
 b^2 - 7b + 9 \\
 3b + 7 \overline{) 3b^3 - 14b^2 - 22b + 70} \\
 \underline{3b^3 + 7b^2} \phantom{- 22b + 70} \\
 -21b^2 - 22b \phantom{+ 70} \\
 \underline{-21b^2 - 49b} \phantom{+ 70} \\
 27b + 70 \\
 \underline{27b + 63} \\
 7
 \end{array}$$

$$b^2 - 7b + 9 + \frac{7}{3b + 7}$$

3) Describe how the remainder theorem helps us determine the points on a polynomial graph?

*If you divide a polynomial by synthetic division, the number dividing by is the x coordinate and the remainder is the y coordinate*

4) List all of the possible rational zeros for the following polynomials:

a.  $f(x) = x^3 - 27$

$x = \pm 1, \pm 3, \pm 9, \pm 27$

b.  $f(x) = 2x^4 - 9x^2 + 7$

$x = \pm 1, \pm 7, \pm \frac{1}{2}, \pm \frac{7}{2}$

c.  $f(x) = 3x^4 - 10x^3 - 24x^2 - 6x + 5$

$x = \pm 1, \pm 5, \pm \frac{1}{3}, \pm \frac{5}{3}$

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5) Simplify the following complex expressions:

a.  $-3 + 6i - (-5 - 3i) - 8i$

$$-3 + 6i + 5 + 3i - 8i$$

$$\boxed{2 - i}$$

b.  $(7 - 6i)(-8 + 3i)$

$$-56 + 21i + 48i - 18i^2$$

$$-56 + 69i + 18$$

$$\boxed{-38 + 69i}$$

c.  $\frac{-3 - 7i}{7 + 10i}$

$$\frac{-3 - 7i}{7 + 10i} \cdot \frac{7 - 10i}{7 - 10i} = \frac{-21 + 30i + 49i - 70i^2}{49 - 100i^2} = \frac{-21 + 79i + 70}{149}$$

~~$$\frac{-91 - 19i}{149}$$~~

$$\boxed{\frac{-21 + 79i + 70}{149}}$$

d.  $\frac{-10 - 5i}{-6 + 6i} \cdot \frac{-6 - 6i}{-6 - 6i} = \frac{60 + 60i + 30i + 30i^2}{36 - 36i^2}$

$$= \frac{30 + 90i}{72} = \boxed{\frac{5 + 15i}{12}}$$

6) Find the real zeros of the following polynomials:

a.  $f(x) = 3x^4 - 20x^3 + 26x^2 - 4x - 5$

$$\boxed{x = 1 \text{ mult } 2, 5, -\frac{1}{3}}$$

b.  $f(x) = 6x^3 + 7x^2 - 1$

$$\boxed{x = -1, -\frac{1}{2}, \frac{1}{3}}$$

c.  $f(x) = 2x^4 - x^3 - 18x^2 + 9x$

$$\boxed{x = 0, \frac{1}{2}, 3, -3}$$

$$x(2x^3 - x^2 - 18x + 9)$$

$$x(x^2(2x-1) - 9(2x-1))$$

$$x(2x-1)(x^2-9)$$

$$x(2x-1)(x+3)(x-3)$$