## **Lesson 1.5 - Defining Increasing and Decreasing Intervals**

Learning Objectives: SWBAT

- · Define increasing and decreasing intervals of a function graph
- · Identify the existence of relative maxima/minima of a function given its graph

## <u>Review</u>: Identifying Increasing/Decreasing Intervals

- An interval of a function is INCREASING if its slope is positive
- An interval of a function is DECREASING if its slope is negative
- An interval of a function is CONSTANT if its slope is zero
- Always define increasing/decreasing intervals using "x" values (look left to right)
- See the figure below for each case



- This function is decreasing on the interval [-2, 0]
- This function is constant on the interval [0, 2]
- This function is increasing on the interval [2. 4]

Your Turn: Define the increasing/decreasing/constant intervals for the following:





 $f(x) = \begin{cases} x+1, & x < 0\\ 1, & 0 \le x \le 2\\ -x+3 & x > 2 \end{cases}$ 

## Review: Relative Maxima/Minima

- A relative Maxima (max) is a turning point on a graph where the slope goes from **positive to negative**. The slope at the point itself is zero
- A relative Minima (min) is a turning point on a graph where the slope goes from **negative to positive**. The slope at the point itself is zero



## Lesson 1.5 - Defining Increasing and Decreasing Intervals

Practice: Use DESMOS to graph each function. After graphing determine the intervals upon which the function is increasing, decreasing or constant

**23.** 
$$f(x) = 3$$
 **24.**  $f(x) = x$  **25.**  $f(x) = x^{2/3}$ 

**27.** 
$$f(x) = x\sqrt{x+3}$$
 **28.**  $f(x) = \sqrt{1-x}$  **29.**  $f(x) = |x+1| + |x-1|$ 

1) 
$$y = -x^3 + 2x^2 + 2$$
  
2)  $y = x^3 - 11x^2 + 39x - 47$   
3)  $y = -x^4 + 3x^2 - 3$ 

Practice: Use DESMOS to graph each function. After graphing use DESMOS to determine the coordinates of any relative maxima/minima

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**31.** 
$$f(x) = x^2 - 6x$$
 **32.**  $f(x) = 3x^2 - 2x - 5$  **33.**  $y = 2x^3 + 3x^2 - 12x$ 

**34.** 
$$y = x^3 - 6x^2 + 15$$
 **35.**  $h(x) = (x - 1)\sqrt{x}$  **36.**  $g(x) = x\sqrt{4 - x}$ 

**37.** 
$$f(x) = x^2 - 4x - 5$$
 **38.**  $f(x) = 3x^2 - 12x$  **39.**  $f(x) = x^3 - 3x$