For the functions below:

- Determine/state the excluded values and domain of the function
- Determine/state the location of any vertical, horizontal or slant asymptotes
- · Determine/state the coordinates of any holes
- Determine/state the coordinates of any x intercepts
- · If any of the above does not exist on the graph, please say so

1)
$$f(x) = \frac{x^3 - 4x}{x^2 - 3x - 10}$$

2)
$$f(x) = \frac{4x^2 - 13x + 3}{x^2 + 8x - 33}$$

Solve the following equations, Please note any extraneous solutions

1)
$$1 = \frac{n-2}{n-1} + \frac{3}{n^2 + 3n - 4}$$

2)
$$1 = \frac{2}{r^2} - \frac{1}{r}$$

Solve the following inequalities, quantify your answer in interval notation

3)
$$(x + 4)^2(x - 1)^2(x - 6) < 0$$

4)
$$4m^3 + 7m^2 - 2m > 0$$

5)
$$\frac{4}{x-1} \ge \frac{3}{x-7}$$

6)
$$\frac{3}{x-2} \le \frac{3}{x+3}$$

Simplify the following:

25)
$$(-3+3i)^2$$

26)
$$(-3+6i)(5-6i)$$

29)
$$(3i)(-3-4i)(7-5i)$$

30)
$$(-7i)(-2+7i)(2+6i)$$

39)
$$\frac{-7+i}{-6-8i}$$

40)
$$\frac{-2+i}{-1-8i}$$

37)
$$\frac{8}{-4-2i}$$

$$38) \ \frac{6i}{9-9i}$$

Solve the following for all real/complex solutions

1)
$$x^4 - 5x^2 - 36 = 0$$

2)
$$x^3 + 3x^2 - 14x - 20 = 0$$

5)
$$x^4 + 6x^2 + 8 = 0$$

9)
$$x^3 - 2x^2 - 3x + 6 = 0$$

Write the equation of the polynomial that has the following zeros:

a.
$$-3 \text{ mult. 2}, \ 2\sqrt{2}$$

b.
$$-3 + 2i$$
, $-2 - 2i$

Use the zero(s) given to determine all other zeros to the polynomial equation:

a.
$$f(x) = x^4 - 3x^3 + 6x^2 + 2x - 60$$
; $1 + 3i$

b.
$$g(x) = x^3 - 7x^2 - x + 87$$
 5 + 2i

$$5 + 2i$$

- What is the difference between a real and a complex number. Give an example of each
- What is the relationship between the domain of a rational function and its discontinuities? What are the two types of discontinuities that can be present on a rational function graph?

• What is an extraneous solution? What types of functions have extraneous solutions and why? Describe how you can check for extraneous solutions

• Describe how to find the location of a Horizontal Asymptote of a rational function

Factor each to linear factors. One zero has been given.

19)
$$f(x) = 5x^5 + 49x^4 + 125x^3 + 113x^2 + 22x - 10$$
; $-4 + \sqrt{6}$

Solve the following AV equations, identify any extraneous solutions

a.
$$-3|x-1|-6=3$$

b.
$$\frac{1}{4}|2x-6|+1=2$$

c.
$$|2x + 3| = 3x + 2$$

d.
$$-5|3+4k|=-115$$

Solve the following AV inequalities and graph the solution on a number line.

a.
$$2|x-9|+6>6$$

b.
$$3\left|\frac{1}{2}x+2\right|+6 < 15$$

$$|c. -4|3x - 1| \ge 8$$

d.
$$\frac{\left|2+3x\right|}{2} \ge 5$$